Measuring genomic pre-selection in theory and in practice

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In Theory

- Traditional mixed models do not account for genomic selection
 - Phenotypes only for animals with highest Mendelian sampling
 - GBV differ from EBV for progeny, mates, parents, or herdmates
- Multi-step methods may be biased
- Single-step methods reduce bias



1-Step Relationship Inverse

Aguilar et al. (2010)

$$H^{-1} = \begin{bmatrix} A^{11} & A^{12} \\ A^{21} & A^{22} + G^{-1} - A_{22}^{-1} \end{bmatrix}$$

1 = non-genotyped animals (60 million) 2 = genotyped animals (400,000)



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Traditional and 1-Step Models

- > Animal model
 - **EBV** = $w_1 PA + w_2 YD + w_3 PC$
 - (parent average, yield deviation, progeny contribution)
- > 1-step genomic info (GI) model
 - **GBV** = $w_1 PA_g + w_2 YD_g + w_3 PC_g + w_4 GI$
 - GI = $\sum \text{off-diagonal}_j \text{ of } \text{G}^{-1} \text{A}_{22}^{-1} (\text{GBV}_j)$ divided by diagonal_i of $\text{G}^{-1} - \text{A}_{22}^{-1}$
 - Numerator of w₄ in denominator of w



Diagonals of G⁻¹–A₂₂⁻¹

- Computed for 8,300 Brown Swiss
- Diagonals of G and A₂₂ are similar
 - G: mean $F_G = 3.98\%$ and SD = 4.15%
 - A₂₂: mean F_A = 3.95% and SD = 2.97%
- Diagonals of G⁻¹ larger than A₂₂⁻¹
 - Mean = 5.83 for G, 2.18 for A₂₂
 - G⁻¹, A₂₂⁻¹ and difference all highly correlated



Correlations of Diagonals

Genotyped Brown Swiss

	G	Α	G -1	A -1	G ⁻¹ - A ⁻¹
G	1.0	.70	.05	.03	.06
Α		1.0	.02	02	.04
G ⁻¹			1.0	.98	.99
A -1				1.0	.94
G ⁻¹ - A ⁻¹					1.0



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Simulations of Pre-Selection Bias

- Phenotyped only animals with good Mendelian sampling genotypes
- Discrete or overlapping generations
 - Bias if discrete (Patry, Ducrocq 2011)
 - OK with overlap (Nielsen et al, 2012)
 - Large bias for dams (Liu et al, 2009)
- > Actual studies of pre-selection and genomic assortative mating needed



In Practice

- > Test actual selection and mating
- > Quantify genomic pre-selection in:
 - Mates of proven bulls (group 1)
 - Mates of young bulls (group 2)
 - Dams of young selected sons
- Measure future bias because preselection has already occurred



Percentage of Genotyped Mates Group 2 bulls ranked by NM\$





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Mates of Group 1 and 2 Bulls

- > Group 1 (proven bulls)
 - Daughters with records
 - Top 50, no dtrs in April 2010
 - Were mates pre-selected?
- » Group 2 (young bulls)
 - Top 50, born 2009 and 2010
 - Study calves born in USA





Will pre-selected mates cause bias?



Group 1 Realized Mate Bias

Trait	Mean	SD	Min	Max
NM\$	2	4	-5	13
Protein	0	0	-1	1
Prod Life	.0	.0	.0	.1
Dtr Preg Rate	.0	.0	.0	.1
SCS	.00	.00	01	.01
Final Score	.00	.01	04	.02
Udder Depth	.00	.01	02	.02



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Group 2 Future Bias from Mates

Trait	Mean	SD	Min	Max
NM\$	8	9	0	33
Protein	0	0	0	1
Prod Life	.1	.1	.0	.5
Dtr Preg Rate	.1	.1	.0	.3
SCS	01	.01	03	.00
Final Score	.02	.03	01	.10
Udder Depth	.03	.04	01	.13



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Future Bias – Dams of Young Bulls

- Dams with ≥ 1 sampled son born 2008 to 2012
- Son selection differential = ∑(GPTA – PA) / # of sons sampled
- Dam's bias = 2 * sons' selection differential * (DE from sampled sons) / (total conventional DE)
 - DE = daughter equivalents or EDC





- > 29 sons genotyped, 6 selected, each will provide 5.4 DE
- Son selection differential for milk = ∑(GPTA – PA) / 6 = 583 pounds
- > 30 daughters, each provide 1.5 DE
- > 8.3 DE from PA, 7.8 from records
- Dam's future bias = 2 * 583 * 6 * 5.4 / [8.3 + 7.8 + 6 * 5.4 + 30 * 1.5] = 808



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Expected Future Bias – Bull Dams

Trait	Mean	SD	Min	Max
NM\$	29	33	-124	156
Protein	1	3	-10	14
PL	.3	.5	-1.7	2.0
DPR	.1	.2	9	.9
SCS	01	.04	22	.14



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Potential Biases

- > Also from preferential treatment
 - High-priced early daughters
 - Lack of random sampling

Deregression removes some bias

- Example: dam gets credit only for own records and non-genotyped progeny, not genotyped sons
- Use matrix instead of simple one at a time deregression



Conclusions

- Evaluations should adjust for GBV instead of EBV of:
 - Progeny, mates, contemporaries, and parents
- » Biases from pre-selection:
 - Very small for recently proven bulls
 - Moderate from mates top young bulls
 - Will be large for dams of several highly selected sons, but deregression can remove some of the bias



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